

CompSci 260P: Week 4

Midterm Preparation

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Before We Begin

- Hi, my name is Ryuto Kitagawa, and I'm one of your TA's :)
- Office Hours: Mondays from 2:00 - 5:00pm at ICS 458F
- Next week Thursday is Midterm

Ring Problem

- Suppose you are given a ring which looks like the one shown below
- Each step, you may turn the ring one letter or press the button
- Let K be a word you want to spell
 - What is the minimum number of steps necessary to spell K ?

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Ring Problem: Solution

- Observation: Can we represent this as a graph?
- What would be a natural start to our graph?
 - Let start of string be the first node in our graph
- What would the adjacent nodes be?
 - The next letter in K !
 - Note: You could make it the adjacent letters in the ring, which is a valid solution, but less efficient
- Should the graph be weighted or unweighted?
 - Weighted by number of steps it takes to enter that letter
- How do we find the answer in this graph?
 - Use Dijkstra to find the shortest path!

Recursion Fundamentals

- Recursion is the core of dynamic programming
- Make the problem smaller in some way
 - What that means depends on the problem!
- Smaller problem is input to your algorithm
 - Assume output here is correct!
- These two key points should shape what your recursive algorithm looks like
- **Don't forget the base case!**

Recursion Fundamentals

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Dynamic Programming Fundamentals

- Dynamic Programming is the natural extension of a recursive algorithm
- Do not redo computations!
 - Find repetitive computations and stop them
 - Find the order of dependencies to linearize the algorithm
- This takes time to understand!



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- Suppose you are organizing a company party
- The corporation has a hierarchy tree
 - An employee has some subordinates, who have some subordinates, etc.
 - Creates a hierarchy tree
- If an employee is invited, their immediate supervisor cannot be invited
- Each employee i has a value v_i for how much value they bring to the party
 - Note: Assume the people organizing this party are jerks
- Produce an algorithm which maximizes the value of the party

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Company Party: Recursive Solution

- Consider the tree containing the hierarchy of all employees
- Start with the root:
 - Can you make a decision on this employee?
 - Invite, or don't invite!
- What about the root's children?
 - If we invited the root, then we can *not* invite them!
- Pass valid subtrees into the recursive function!

- How do we linearize the algorithm?
 - Solve the base case first!
 - Then solve the next dependent parts
- Compute the function starting with the leaves
 - Solve all nodes at the lowest height
 - Then solve nodes one level above
 - Keep going all the way to the top!